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**ON THE CLASSIFICATION OF A FIRST ORDER SMOOTH  
THRESHOLD AUTOREGRESSIVE (STAR) MODEL**

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**Summary**

This paper establishes a necessary and sufficient condition for recurrence and ergodicity for the general first-order smooth threshold autoregressive processes. Depending on the tail behaviour of the smoothing distribution function, we give necessary and sufficient conditions under which the process is ergodic, null recurrent or transient.

**Keywords:** Nonlinear time series, Smooth Threshold Autoregressive model, Ergodic, Null recurrent, Transient.

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